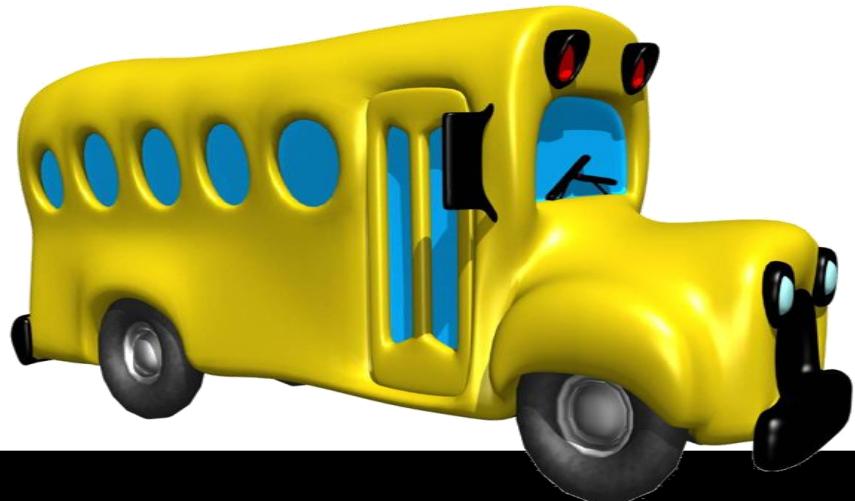


# **Bab 2**

# **Bagian 2**

## Ukuran Sebaran



Don't worry about the dinner,  
Mother. When you have an oven  
with a lower standard deviation,  
you'll never burn anything again.

Not everything's reliable, but how can u tell?

Average do a great job of giving u a  
typical value in your data set,  
but they don't tell u the full story

→are'nt enough information  
in summarizing a data set



# Ukuran sebaran

- Variabilitas → ukuran kuantitatif yang menunjukkan seberapa jauh data dalam suatu distribusi menyebar
- Jika  $X$  sangat dekat dengan rata-rata → rata-rata menjadi ukuran yang baik
- Seberapa “jauh” suatu data dari rata-rata? (Misalkan rata-rata adalah “**best guess**”)



The Statsville  
All Stars coach

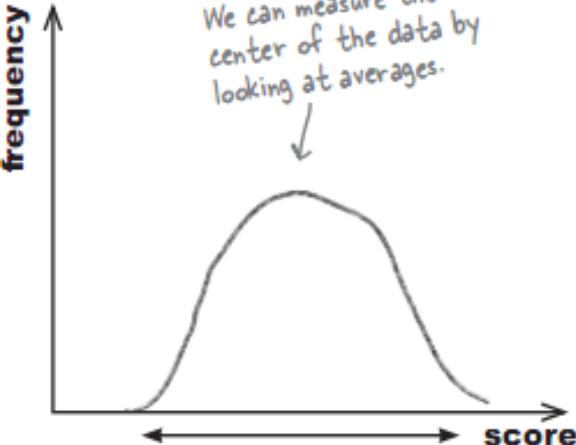


All three players have  
the same average score  
for shooting, but I need some  
way of choosing between them.  
Think you can help?

All three players had  
the same average  
score in the trials,  
so how should the  
coach decide which  
to pick?



## Basketball player scores



The mean tells us nothing about how spread out the data is, so we need some other measure to tell us this.



Points scored per game	7	9	10	11	13
Frequency	1	2	4	2	1

Misal:  
data berisi tentang skor poin per-permainan



Points scored per game	7	8	9	10	11	12	13
Frequency	1	1	2	2	2	1	1

Here, frequency tells us the number of games where the player got each score. This player scored 9 points in 2 games, and 12 points in 1 game.



Points scored per game	3	6	7	10	11	13	30
Frequency	2	1	2	3	1	1	1

# 1. Rentang (Range)

Range is a way of measuring how spread out a set of values are.

- Untuk data tak berkelompok

$R = \text{Nilai Maks} - \text{Nilai Min}$

- Untuk data berkelompok

$R = \text{Nilai tengah kelas terakhir} - \text{Nilai tengah kelas pertama}$

$R = \text{Batas atas kelas terakhir} - \text{Batas bawah kelas pertama}$



# contoh

Kelas		Titik Tengah M	Frekuensi
BB	BA		
30	39	34.5	2
40	49	44.5	3
50	59		11
60	69		20
70	79		32
80	89		25
90	99		7

Rentang = 60

Rentang = 69



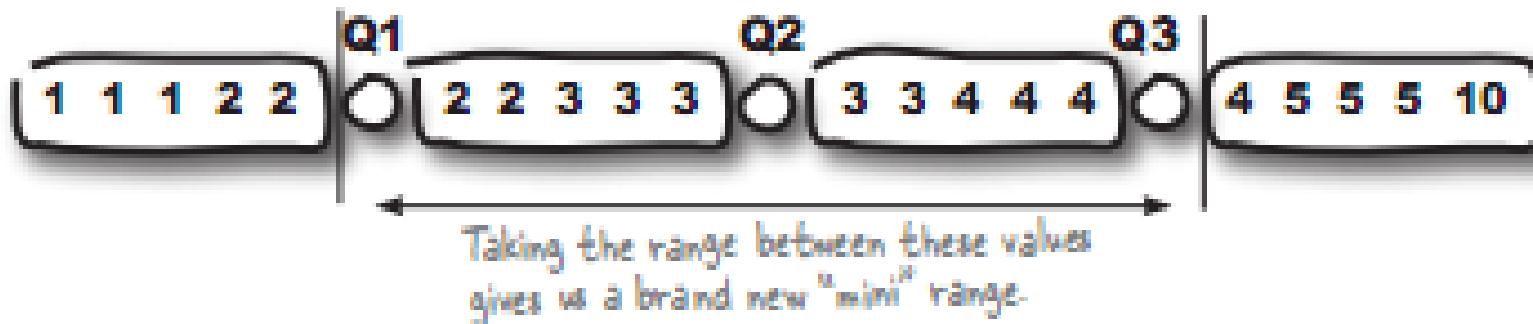
## Range... cont

- Range → cara mudah mencari ukuran penyebaran suatu data namun “sering bukan yang terbaik”
- Jika data berisi outlier, range bisa jadi *misleading* sebagai ukuran penyebaran karena sensitif terhadap outlier



# Masalah ... dengan Range ...

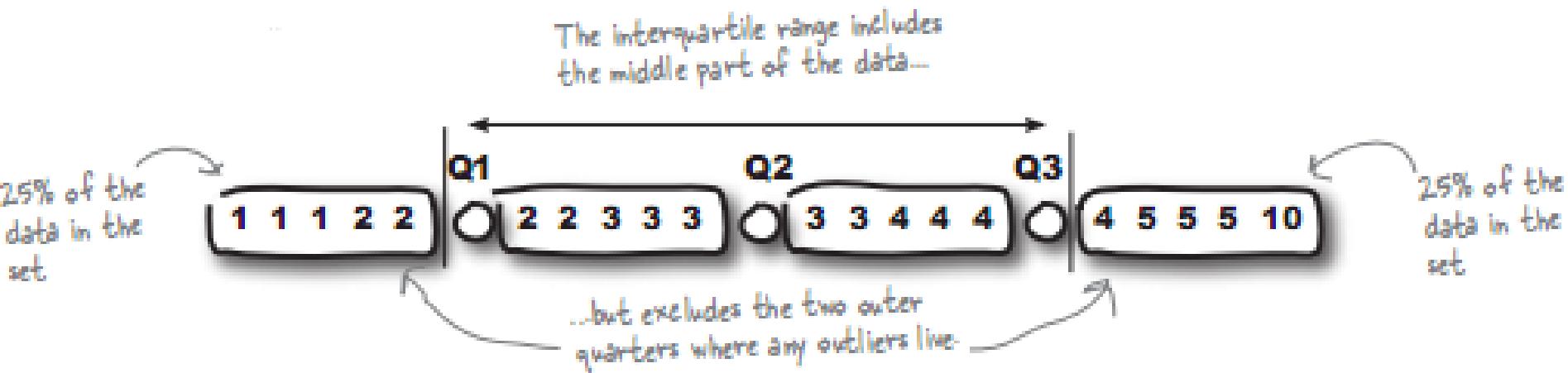
- Mendeskripsikan lebar data
- Sensitif terhadap outlier → alternatif : mini range ; quartile



## 2. IQR

Alternatif lain ... → IQR

- Lot less sensitive then range



$$\text{IQR} = Q_3 - Q_1$$



# Pagar Dalam & Pagar Luar

$$IF = Q_1 - 1.5(IQR) \quad \& \quad Q_3 + 1.5(IQR)$$

$$OF = Q_1 - 3(IQR) \quad \& \quad Q_3 + 3(IQR)$$



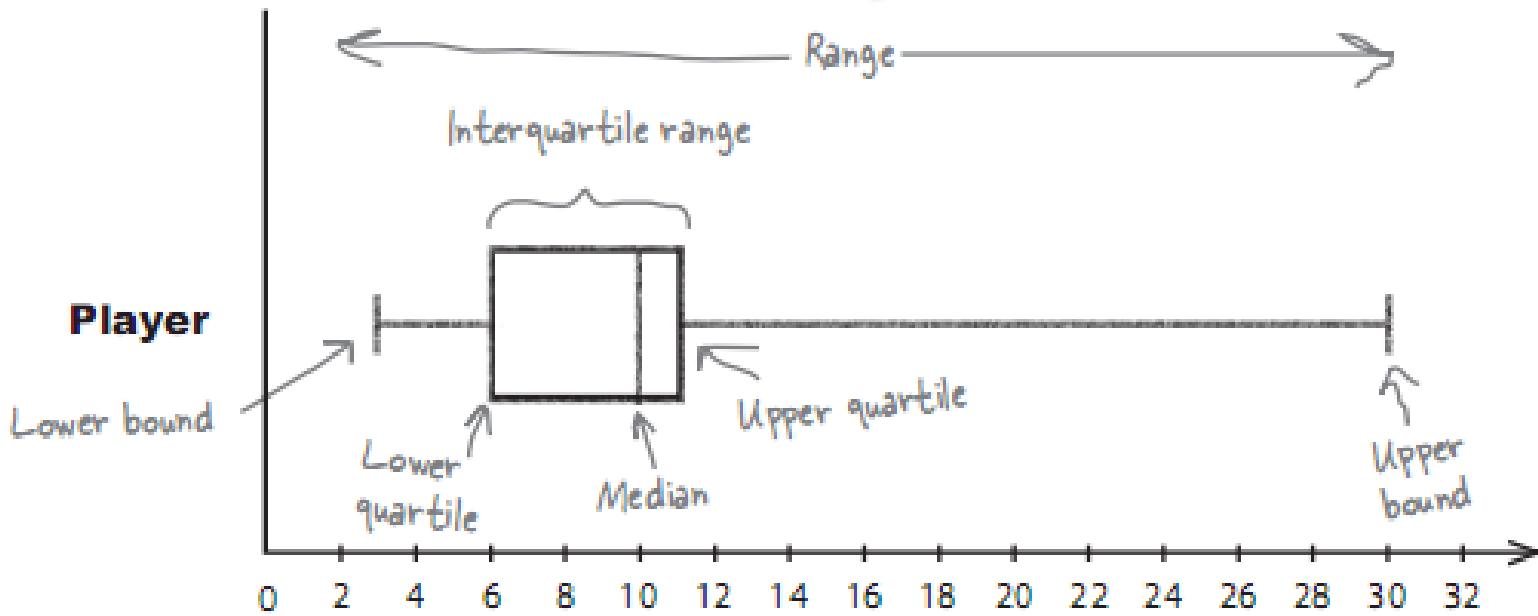
# BOX PLOT



Here's a reminder of  
the data.

3 3 6 7 7 10 10 10 11 13 30

Basketball player scores





Work out the mean, lower bound, upper bound, and range for the following sets of data, and sketch the charts. Are values dispersed in the same way? Does the range help us describe these differences?

Score	8	9	10	11	12
Frequency	1	2	3	2	1

Score	8	9	10	11	12
Frequency	1	0	8	0	1

Hitung rata-rata, range dari data pada Tabel di atas.

Apakah nilai-nilai data mempunyai simpangan yang sama?

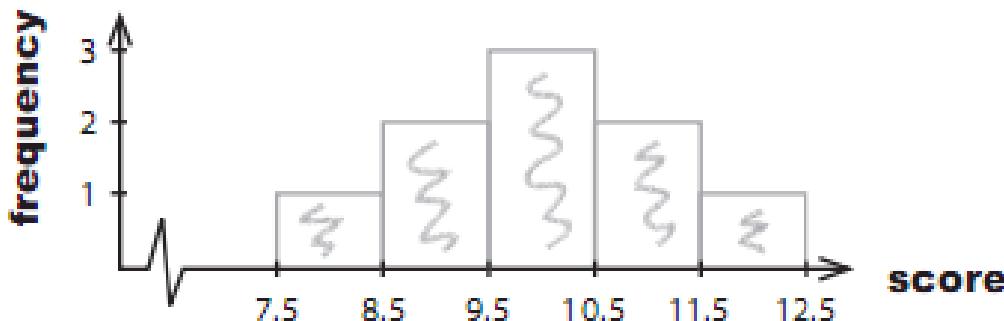
Apakah Range dapat membantu kita dalam menggambarkan penyebaran ini?





Work out the mean, lower bound, upper bound, and range for the following sets of basketball scores, and sketch the charts. Are values dispersed in the same way? Does the range help us describe these differences?

Score	8	9	10	11	12
Frequency	1	2	3	2	1



$$\mu = 10$$

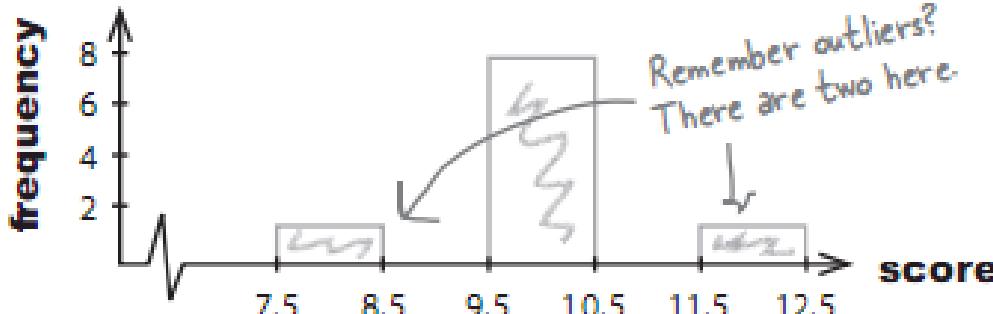
$$\text{Lower bound} = 8$$

$$\text{Upper bound} = 12$$

$$\begin{aligned}\text{Range} &= 12 - 8 \\ &= 4\end{aligned}$$

Look, these results are the same even though the data's different.

Score	8	9	10	11	12
Frequency	1	0	8	0	1



$$\mu = 10$$

$$\text{Lower bound} = 8$$

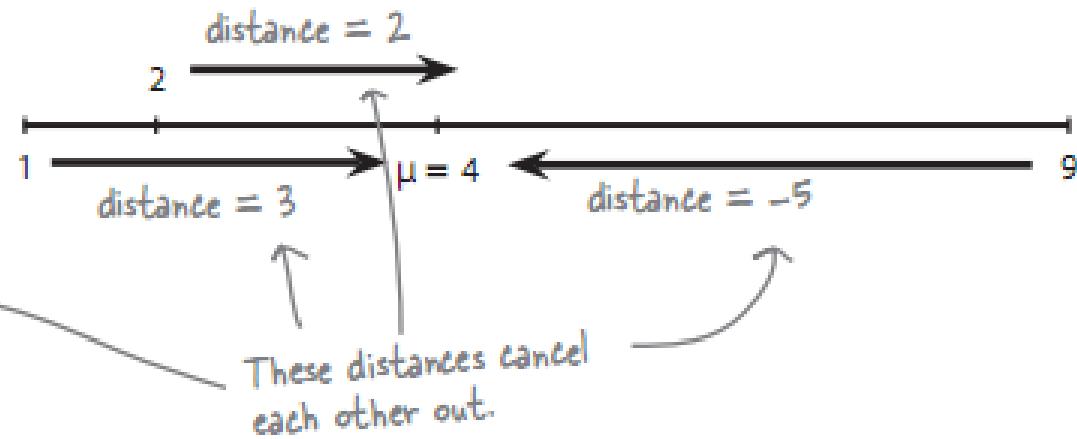
$$\text{Upper bound} = 12$$

$$\begin{aligned}\text{Range} &= 12 - 8 \\ &= 4\end{aligned}$$

### 3. Variansi

Misal kita punya data 1, 2 dan 9 dengan rata-rata =4. Berapakah *average jarak* data tsb dari rata-ratanya ?

$$\begin{aligned}\text{Average distance} &= \frac{(1 \text{ to } \mu) + (2 \text{ to } \mu) + (9 \text{ to } \mu)}{3} \\ &= \frac{3 + 2 + (-5)}{3} \\ &= 0\end{aligned}$$



# ... Variansi

→ Deviasi dari satu observasi pengukuran thp rata-rata

## Populasi

$$\sigma^2 = \frac{\sum_{i=1}^n (X_i - \mu)^2}{N} = \frac{\sum_{i=1}^n X_i^2}{N} - \mu^2 \Rightarrow \sigma = \sqrt{\frac{\sum_{i=1}^n (X_i - \mu)^2}{N}}$$

## Sampel

$$s^2 = \frac{\sum_{i=1}^n (X_i - \bar{x})^2}{n-1} \Rightarrow s = \sqrt{\frac{\sum_{i=1}^n (X_i - \bar{x})^2}{n-1}}$$



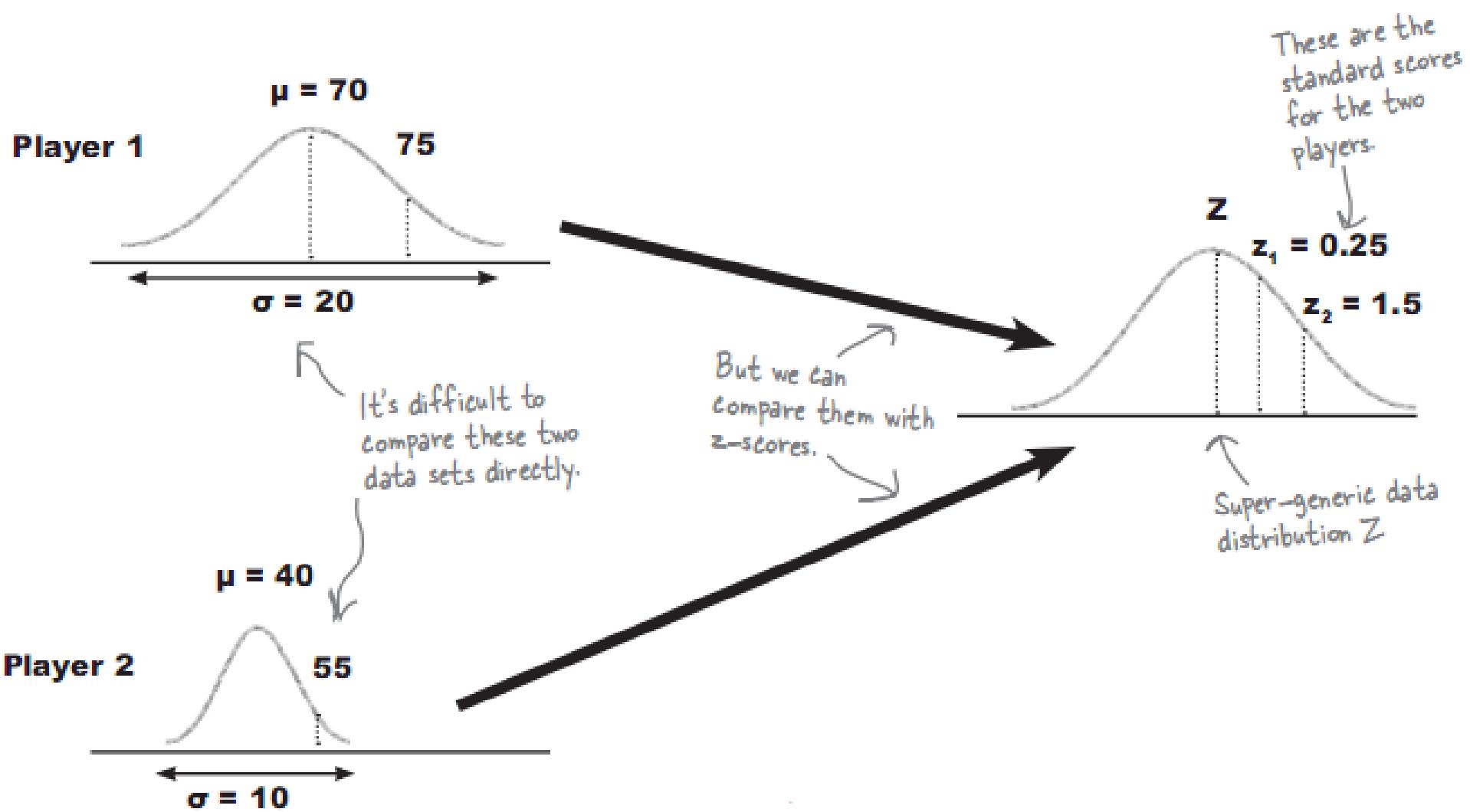
# Nilai Standar (Baku)

Nilai Standar (baku) memberikan cara dalam perbandingan suatu nilai apabila nilai tersebut berasal dari himpunan atau distribusi yang sama.

$$z = \frac{x - \mu}{\sigma}$$



# Ilustrasi



Which players better ?

# Latihan

Seorang pelatih basket mempunyai record pertandingan 3 pemain. Rata-rata tiap pemain adalah 10. Jika pelatih juga menghitung ukuran simpangan pemain-pemain itu. Menurut Anda pemain mana yang paling reliabel untuk dapat dipilih?

Player 1

Score	7	9	10	11	13
Frequency	1	2	4	2	1

Player 2

Score	7	8	9	10	11	12	13
Frequency	1	1	2	2	2	1	1

Player 3

Score	3	6	7	10	11	13	30
Frequency	2	1	2	3	1	1	1



Do U have same conclusion when U work out with Range ?